

Spiral Review:

Complete the square.

$$1.) x = y^2 - 14y + 25$$
$$\begin{array}{r} -25 \qquad \qquad -25 \\ \hline x - 25 = y^2 - 14y + 49 \\ \boxed{x + 24 = (y - 7)^2} \end{array}$$

$$2.) x^2 + y^2 + 8x - 6y = 0$$
$$\begin{array}{r} x^2 + 8x + 16 + y^2 - 6y + 9 = 0 + 16 + 9 \\ \boxed{(x + 4)^2 + (y - 3)^2 = 25} \end{array}$$

$$3.) x^2 + 4y^2 + 4x - 24y + 24 = 0 \quad 4.) 4x^2 - 9y^2 - 32x - 18y + 19 = 0$$

$$x^2 + 4x + 4 + 4y^2 - 24y = -24$$

$$x^2 + 4x + 4 + 4(y^2 - 6y + 9) = -24 + 4 + 36$$

$$\frac{(x+2)^2}{16} + \frac{4(y-3)^2}{16} = \frac{16}{16}$$

$$\boxed{\frac{(x+2)^2}{16} + \frac{(y-3)^2}{4} = 1}$$

$$4x^2 - 32x - 9y^2 - 18y = -19$$

$$4(x^2 - 8x + 16) - 9(y^2 + 2y + 1) = -19 + 64 - 9$$

$$\frac{4(x-4)^2}{36} - \frac{9(y+1)^2}{36} = \frac{36}{36}$$

$$\boxed{\frac{(x-4)^2}{9} - \frac{(y+1)^2}{4} = 1}$$

p.636 9.1 Circles

Formula:

$$(x - h)^2 + (y - k)^2 = r^2$$

Center: (h,k)

radius: r

Don't forget- radius is half the diameter!

Students will be able to find the standard form of the equation of the circle.

Example 1: Find the standard form of the equation of the circle with the given characteristics.

a.) center: origin $(0,0)$
radius: $\sqrt{11}$

$$(x-0)^2 + (y-0)^2 = (\sqrt{11})^2$$

$$\boxed{x^2 + y^2 = 11}$$

b.) center: $(6, -3)$
point on circle: $(-2, 4)$

$$d = \sqrt{(6 - (-2))^2 + (-3 - 4)^2}$$

$$= \sqrt{(8)^2 + (-7)^2}$$

$$= \sqrt{64 + 49}$$

$$d(r) = \sqrt{113}$$

$$(x-6)^2 + (y-(-3))^2 = (\sqrt{113})^2$$

$$\boxed{(x-6)^2 + (y+3)^2 = 113}$$

Students will be able to identify the center and radius of the circle.

Example 2: Identify the center and radius of the circle.

a.) $x^2 + y^2 = 121$

$$\text{center} = (0, 0)$$

$$\text{radius} = \sqrt{121} \\ = 11$$

b.) $x^2 + (y + 8)^2 = 25$

$$\text{center} = (0, -8)$$

$$\text{radius} = \sqrt{25} \\ = 5$$

Students will be able to write the equation of the circle in standard form, identify the radius and center, and sketch.

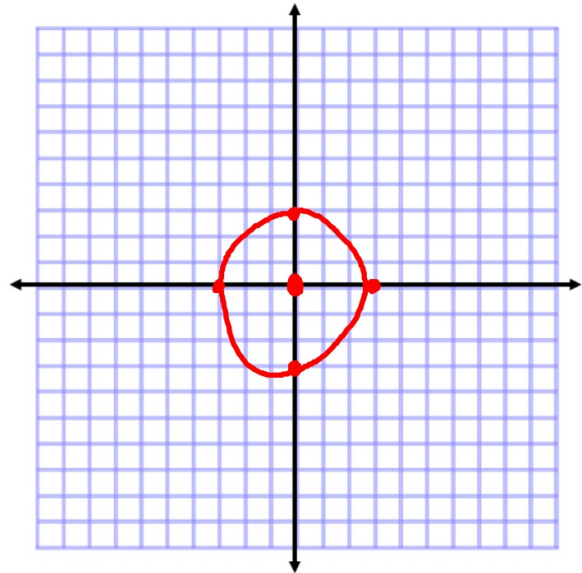
Example 3: Write the equation of the circle in standard form, identify the radius and center, and sketch.

$$a.) \left(\frac{1}{9}x^2 + \frac{1}{9}y^2\right) = (1) \cdot 9$$

$$x^2 + y^2 = 9$$

center: $(0,0)$

$$\text{radius} = \sqrt{9} = 3$$

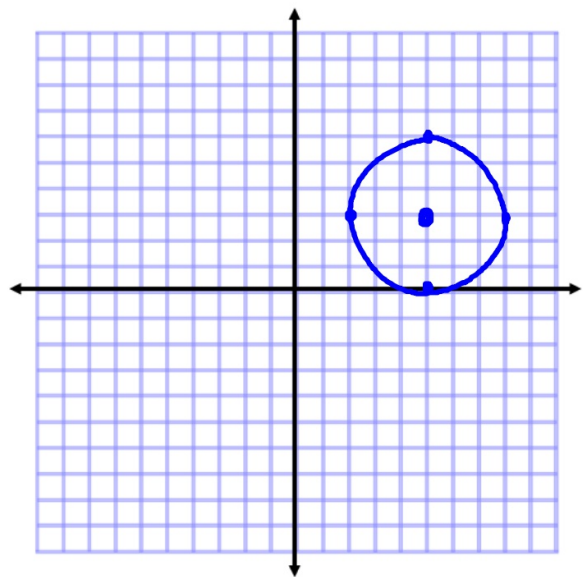


$$b.) x^2 + y^2 - 10x - 6y + 25 = 0$$

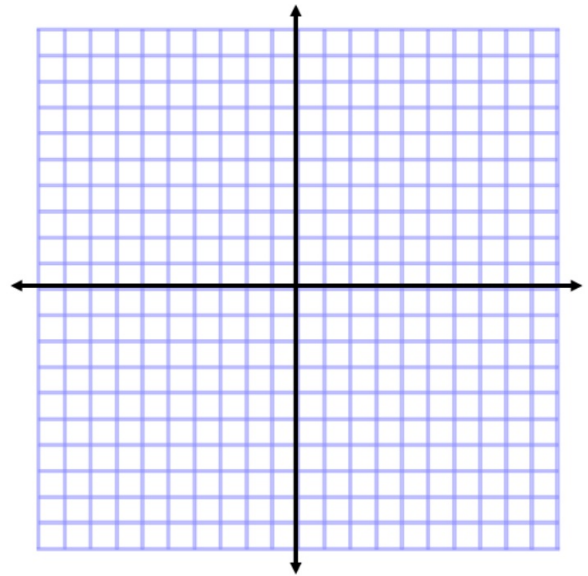
$$(x^2 - 10x + 25) + (y^2 - 6y + 9) = \frac{-25}{+9} + \frac{-25}{+9}$$

$$(x-5)^2 + (y-3)^2 = 9$$

center: $(5,3)$
radius: 3



c.) $y^2 = 81 - x^2$



d.) $x^2 + y^2 + 10y + 9 = 0$

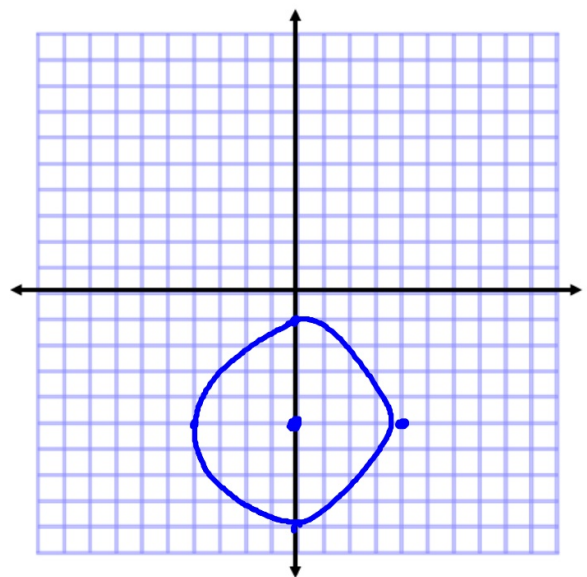
$$x^2 + y^2 + 10y = -9$$

$$x^2 + y^2 + 10y + 25 = -9 + 25$$

$$x^2 + (y+5)^2 = 16$$

Center: $(0, -5)$

Radius: $\sqrt{16} = 4$



Turn-in:

p.643 (18, 22, 30, 32)

HW:

p.643 (7-33 odds, 41, 42)